



A.Y. 2024/2025

BLAB

HANDOUTS

CORPORATE FINANCE

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This handout is written by students with no intention of replacing university materials.

It is a useful tool for studying the subject, but does not guarantee preparation as exhaustive and complete as the material recommended by the University.





1 NOTES

Investment decisions=Capital Budgeting decision

2 LECTURE 1

The objective in **Corporate finance** is maximizing value

Investment decision: Invest in assets that earn a greater return than the minimum acceptable hurdle rate. The hurdle rate reflects the riskiness of the investment and the mix of debt and equity used to fund it. The return should reflect the magnitude and the timing of cashflows as well as all side effects

Financing Decisions: Finding right kind of debt and right mix of debt and equity to fund operations. Includes reinvesting profit. The optimal mix maximizes firm value and the right kind of debt must match the tenor of the assets.

Dividend decision: If no investments that make the minimum acceptable rate, return the cash to owners of the business. The amount returned depends on current and potential investment opportunities and how you choose to return can be dividends or buybacks

6 stages of Growth:

1. **Start-up:** Have idea for a business that meets an unmet need
2. **Young Growth:** Create a business model that converts ideas into potential revenues and earnings
3. **High Growth:** Build the business, convert potential into revenue
4. **Mature Growth:** Shift from losses to profits
5. **Mature Stable:** Defend your business from competition and find new markets
6. **Scale down** your business as market shrinks

In primary markets, prices are usually predetermined, it is generally used to generate equity capital, whereas on the secondary market is generally used by companies to gauge shareholder confidence

Both sole proprietorships and partnerships have unlimited liability and personal tax on profits whereas corporations have limited liability and corporate tax on profits and personal tax on dividends

Agency costs are incurred when managers do not attempt to maximise firm value and shareholders incur cost to monitor the managers and constrain their actions

Board of directors: group of people who represent the interests of a company's shareholders. They also provide guidance and advice to the CEO and executive team. They establish broad policies, explain firm's performance to shareholders, decide on dividends, decide on executive compensation, approve annual budgets, hire and fire top executives, appoint, support and assess the CEO.

A CEO only does three things: Culture, talent, numbers (defining metrics)

Financial manager: Interface between Financial Markets and firm's operations.

When cash is reinvested, the opportunity cost is the expected rate of returns shareholders could have obtained from other financial assets.

If the firm's investments can earn a higher return than the opportunity cost of capital, stock price increases and vice versa. Financial managers can observe the opportunity cost of capital for safe investments by looking at current interest rates on safe debt securities

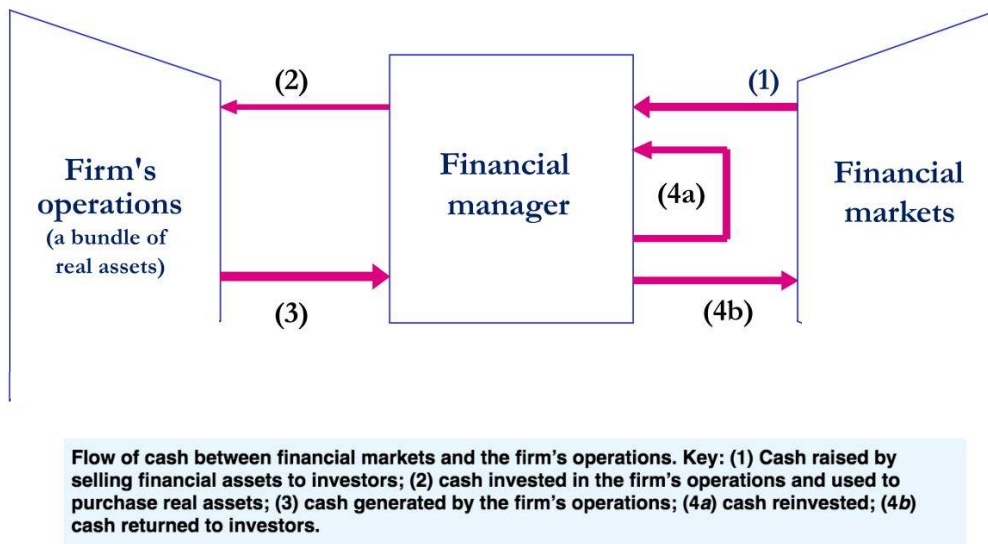


Figure 1: Enter Caption

3 REVISIONS FOR DRAFTKINGS

Discount Cash flows depending on how risky the investment is

You should accept all projects with a positive NPV and reject all projects with a negative NPV. The discount rate represents the highest rate of return (opportunity cost) that investors could obtain in the market in an investment with equal risk

The discounting rate that makes NPV equal to zero is called the "internal rate of return" (IRR) or "yield to maturity"

Accept if $IRR > \text{hurdle rate}$

There can be as many IRRs as there are sign changes

Some companies use the payback rule to help make investment decisions. In other words, they accept only those projects that recover their initial investment within a specified period. Payback ignores the timing of cash flows within the payback period, and it ignores subsequent cash flows entirely. It therefore takes no account of the time value of money.

Rules: Discount CF, not profits (as you need to add back depreciation and subtract capital expenditure to go from accounting profit to cash flow)

You should neither subtract the debt proceeds from the required investment nor recognize the interest and principal payments on the debt as cash outflows

$$\text{Real discount rate} = \frac{1 + \text{nominal discount rate}}{1 + \text{inflation rate}} - 1$$

3.1 LECTURE 5

The longer a bond's maturity, the more affected its price is by changes in interest rate (= to YTM)

$$\text{Duration} = \frac{1 \times PV(C_1)}{PV} + \frac{2 \times PV(C_2)}{PV} + \frac{3 \times PV(C_3)}{PV} + \dots + \frac{T \times PV(C_T)}{PV} \text{ and Modified duration} = \frac{\text{duration}}{1 + \text{yield}} \text{ (It measures the \% change in bond price for a 1\%-point change in yield.)}$$

An increase in coupon rate decreases duration and a decline in yield to maturity increases duration

The yield curve graphs the relationship between bond yields and bond maturity, a normal yield curve is increasing (as higher maturity implies higher risk)

An inverted yield curve has indicated a worsening economic situation in the future 5 out of 6



- You should obtain the same final payoff if you invest by either investing
 - at the 4-year spot rate today, or
 - at the 3-year spot rate today, and then in the forward rate starting in 3 years from now, for one year
- Therefore, we must have

$$(1+s_4)^4 = (1+s_3)^3 \times (1+f_{3,1})$$

This gives:

$$f_{3,1} = 8.51\%$$

- This holds for any maturity (T) and length of forward rate (T-t):

$$(1+s_T)^T = (1+s_{T-t})^{T-t} \times (1+f_{T-t,t})^t$$

times since 1970

The spot rate is the interest rate today for a given maturity t and the forward rate 'interest rate fixed today on a loan made in the future at a fixed time). The latter can be directly observable or be implied in spot rates. Future rates are expected future spot rates

$$1+r = \frac{1+i}{1+\pi}$$

Treasury inflation protected securities (TIP) are securities whose principal is tied to nominal prices. The principal increases with inflation, and at maturity the Treasury pays the greater of the original or the adjusted principal

Bonds with a term shorter than 1 year are called commercial papers, those with more are called corporate bonds

Bonds can have a fixed or variable coupon rate (floaters and inverse floaters)

The putability of a bond is whether the bondholder can demand payment of the loan before maturity

Bonds rated BBB or above are investment grade and the rest are called high yield/junk bonds

The YTM is equal to the Risk free rate (Swap curve for Euro, US and UK treasuries for their respective currencies) +Credit Spread (Fair value + New Issue premium) are all the factors that determine the risk of the bond

Factors that increase credit Spread are

- Tenor:** The longer the higher the CS
- The rating:** The lower the higher the CS
- The absence of **rating increases** the CS
- The **cyclical nature** of the sector increases the CS
- Subordination** in capital structure increases CS

The Benchmark in the Eurozone is typically the German Bund and in the US it's treasury bills with one or three month maturity

The less safety there is, the bigger the CS

3.2 LESSON 6

The Specialist acts as an auctioneer, matching buyers and sellers in auction market. In dealer markets, trades are done directly between investor and dealer

Payout ratio is the fraction of earnings paid out as dividends and the plowback ratio is the fraction of earnings retained by the firm

The growth rate is the ROE times the plowback ratio (how profitable the RE turn out to be)

Growth enhances company value only if it is achieved by investment in projects with attractive profit opportunities (i.e ROE > k)



4 LECTURE 1

Investment decisions: Investing in assets

Financing decision: Finding the right kind of debt and right mix of debt and equity

Dividend Decision: How much to return to investors and in what way?

On the primary market, prices are usually predetermined

Sole proprietorships and partnerships have unlimited liability and only personal taxes on profits, whereas corporations have limited liability and both corporate and personal tax on dividends. The role of a CEO according to Trey Taylor: Culture, talent recruitment and development and define the metrics to evaluate progress

5 LECTURE 1

Non Cash Working capital= Accounts receivables +Inventories -Accounts payables

Net Financial Position= Total Financial debt-cash and equivalents

An increase in working capital reduces CF in that year and inversely

A shorter working capital cycle is useful as it lets you free up cash for use elsewhere

We use four types of ratios: Liquidity, leverage, activity and profitability

Liquidity:

Current ratio: $\frac{\text{Current Assets}}{\text{Current Liabilities}}$

Quick ratio: $\frac{\text{Cash, Marketable Securities and AR}}{\text{Current Liabilities}}$

Leverage:

Financial leverage: $\frac{\text{Total Assets}}{\text{Total Liabilities}}$

Total Debt/Equity: $\frac{\text{Financial Debt}}{\text{Equity}}$

Total Debt/Total Assets: $\frac{\text{LT Debt}}{\text{Total Assets}}$

Interest Coverage: $\frac{\text{EBIT}}{\text{Interest Expense}}$

NFP/Equity: $\frac{\text{Financial Debt} - \text{Cash and equivalents}}{\text{Equity}}$

Activity Ratios:

Days of Receivables (DSO): $\frac{\text{Accounts Receivable}}{\frac{\text{Sales}}{365}}$

Days of inventories (DSI): $\frac{\text{Inventory}}{\frac{\text{COGS}}{365}}$

Days of Payables (DPO): $\frac{\text{Accounts Payable}}{\frac{\text{COGS}}{365}}$

Asset Turnover: $\frac{\text{Total Sales}}{\text{Total Assets}}$

Inventory Turnover (X): $\frac{\text{COGS}}{\text{Inventory}}$

Working capital cycle (days): $DI + DSO - DPO$

The working capital cycle starts upon payment to creditors and ends when receiving cash

Profitability Ratios:

ROA: $\frac{\text{Net Income}}{\text{Total Assets}}$

ROE: $\frac{\text{Net Income}}{\text{Total Equity}}$ (Equity is measured at end of year (EOY))

ROS: $\frac{\text{Net Income}}{\text{Total Sales}}$ (N.B.: Total sales=Total Revenue, Net Sales excludes returns, discounts and allowances)

Dupont Formula: $\text{ROE} = \text{ROS} \times \text{Asset Turnover} \times \text{Financial leverage} = \frac{\text{Net Income}}{\text{Total Asset}} \times \frac{\text{Revenue}}{\text{Average Total Assets}} \times \frac{\text{Average Total Assets}}{\text{Average Total Equity}}$

6 UNIDENTIFIED INDUSTRIES: CASE

7 LECTURE 4



NPV and IRR are the most popular techniques to evaluate investment projects (75% of CFOs always or almost always use it)

Present Value formulas:

Perpetuity: $\frac{C}{r}$

Annuity that pays a fixed sum: $C * \left[\frac{1}{r} - \frac{1}{r(1+r)^t} \right]$

Growing perpetuity: $PV_0 = \frac{C_1}{r-g}$

Constant growth annuity: $PV = C \left[\frac{1}{r-g} - \frac{(1+g)^t}{(r-g)(1+r)^t} \right]$

NPV of a project: $\sum_{t=1}^n \frac{CF_t}{(1+r)^t} - I_0$

NPV Rule: Accept all projects with a positive NPV, reject all those with a negative one

NPV depends on all forecast CF, so all of them must be taken into account

The discounting rate that makes NPV equal to zero is called the internal rate of return (IRR). Can be calculated through trial and error or Excell with the IRR function

The decision rule for the IRR is that we should accept if $IRR > \text{hurdle rate}$

There can be multiple IRR due to changes in sign

Some companies use the Payback rule: Accept only projects that receiver the initial investment within the payback period and ignores subsequent CF. It also doesn't take time value of money into account

Important: Discount Cash flows, not profits (you need to add back depreciation and subtract capex)

Rules:

- Include the projects effect on **other businesses** of the firm
- Remember salvage value, ignore **sunk costs**, include opportunity costs
- Separate Investment and financing decisions (don't take into account payment of debt)
- Forecast CF after taxes
- Take working capital into account (A change in NWWC is a cash flow)
- Treat inflation consistently (use nominal interest rates to discount nominal cf or real inter- est rates to discount real CF)

remember salvage value, ignore sunk costs, include opportunity costs. Separate Investment and financing decisions (don't take into account payment of debt), forecast CF after taxes. Finally, remember to take into

Real discount rate: $\frac{1+\text{nominal discount rate}}{1+\text{inflation rate}} - 1$

8 LECTURE 5: VALUING BONDS

price of a bond: $P_0 = \sum_{t=1}^T \frac{C_t}{(1+YTM)^t} + \frac{F_t}{(1+YTM)^T}$ and YTM is the rate such that price=0. It's the internal rate of return of an investment in an annual pay bond held until maturity with payments done as scheduled

If data is given in an annual form, for a semi-annual bond divide the ytm and coupon rate by two

If a bond's coupon rate is above the YTM, it sells at a premium

Bonds with different maturities have different IRR

Price sensitivity is linked to the average time you need to wait for payments: $Duration = \frac{1 \times PV(C_1)}{PV} + \frac{2 \times PV(C_2)}{PV} + \frac{3 \times PV(C_3)}{PV} + \dots + \frac{T \times PV(C_T)}{PV}$

Modified duration=volatility= $\frac{duration}{1+yield}$

With a modified duration of 5 for example, a 1% change in YTM results in a 5% change to the bond's price

The yield curve graphs the relationship between bond yields and maturity. A normal yield curve



increases, as bonds with a higher maturity have a higher level of risk

Spot rate: Interest rate today for a given maturity (these constitute the yield curve)

Forward rate: Interest rate, fixed today, on a loan made in the future at a fixed time (the interest rate you will pay tomorrow). These are either directly observable or implied in spot rates

Future rates: expected future spot rates

You should receive the same final payoff if you invest at the 5 year spot rate today or the 3 year spot rate and then in the forward rate starting in 3 years for two year: $(1 + s_T)^T = (1 + s_{T-t})^{T-t} \times$

$$(1 + f_{T-t,t})^t$$

$$1 + r = \frac{1+i}{1+i}$$

Treasury Inflation Protected Securities (TIPS) are securities whose principal is tied to nominal prices (CPI). At maturity, the Treasury pays the original or adjusted principal, whichever is greater
Issuers of bonds can be

- US Treasury/ Government
- States, municipalities and agencies
- Corporations
- Foreign governments

If the term is lower than one it's a commercial paper, if it's higher it's a (corporate) bond

The coupon's period is typically semi-annual, the rate can be fixed or variable, nominal or inflation indexed

Bonds can be risk-free or defaultable

Bonds also have different levels of seniority and security (secured or not). Covenants can also be placed on bonds (restrictions on additional issues, dividends...)

Finally, there can be some option provisions: callability (after a certain period, the issuer has the right to pay back the loan before it matures), putability (After a certain period, the bondholder can demand payment of the loan), convertibility (after a certain period, bondholder has the right to exchange the bond for stock of the issuer)

Default/Credit risk: risk that a debt issuer fails to make the promised payment. They are rated by rating agencies, and bonds rates above BBB are investment grade, those below high-yield/junk bond

$$YTM = \text{Risk Free Rate} + \text{Credit Spread}$$

Risk free rate is determined by the swap curve for the Euro, US Treasuries for the Dollar and UK treasuries for the Pound

Credit Spread comes from Fair Value + New Issue premium, and is all the specific factor that determine the risk of the bond, namely:



The spread widens the lower the safety

9 LECTURE 6: STOCK VALUATION

Preferred stock have no voting rights unless no dividends are paid

Warrants are long-term call options

ADR represent the cross listing decision of non-US firms



The DDM assumes that the intrinsic value of a stock is equal to the PV of all expected future

dividends

$$P_0 = \frac{DIV_1 + P_1}{1+r}$$

Solving for r, we get: $r = \frac{Div_1}{P_0} + \frac{P_1 - P_0}{P_0}$

Finally, we obtain: $P_0 = \sum_{t=1}^n \frac{DIV_t}{(1+r)^t} + \frac{P_n}{(1+r)^n} = \sum_{t=1}^{\infty} \frac{DIV_t}{(1+r)^t}$

The Gordon model is used when dividends are expected to grow at a constant rate g forever, we get: $P_0 = \frac{DIV_1}{r-g} \iff r = \frac{DIV_1}{P_0} + g$

Remember that DIV 1 is different from DIV 0

Preferred stock that pays a fixed dividend can be valued using the constant growth dividend discount model, setting g to 0

The Payout ratio is the fraction of earnings paid out as dividends and the plowback ratio is the fraction of earnings retained by the firm. A higher plowback ratio (b) can increase stock price as higher future dividends are expected

$g = ROE \times b$, substituting it in the equation we get $P_0 = \frac{D_1}{k - ROE \cdot b}$

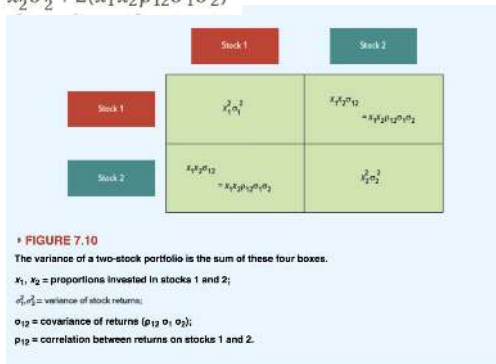
The difference in stock price between the scenario with no plowback and the one with some plowback is the PVGO and we have: $PV_t = \frac{EPS_{t+1}}{r} + PVGO \iff PVGO = P - \frac{EPS_{t+1}}{r}$

Growth enhances company value only if it is achieved by investing in projects with attractive profit opportunities ($ROE > K$)

Two step DDM: $P_0 = \sum_{t=1}^T \frac{Div(1+g)^t}{(1+R)^t} + \frac{Div_{T+1}}{(1+R)}$

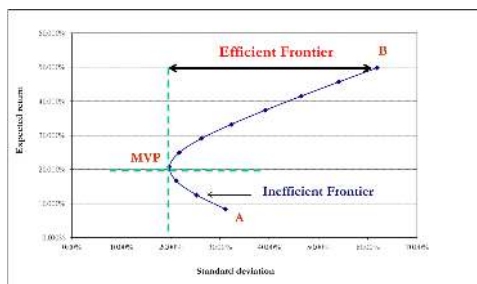
10 LECTURE 9-11

Portfolio variance = $x_1^2 \sigma_1^2 + x_2^2 \sigma_2^2 + 2(x_1 x_2 \rho_{12} \sigma_1 \sigma_2)$



Portfolio variance = $x_1^2 \sigma_1^2 + x_2^2 \sigma_2^2 + 2(x_1 x_2 \rho_{12} \sigma_1 \sigma_2)$

The only case with no gains from diversification is when the correlation is 1



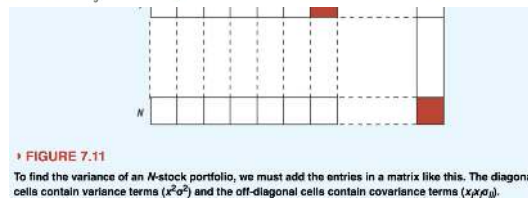


The two finance axioms are investors prefer more to less and are risk-averse
 Only economy wide sources of risk that affect the overall stock market (inflation rate i.e.) cannot be diversified away (systematic risk)
 Because of globalization, correlations across markets and economies are increasing and reducing the effectiveness of diversification. Similarly, securitization increases correlation across classes
 When there is a crisis of confidence and investors become more risk averse, the correlation across risky assets increases thus undercutting the benefits of diversification
 Specific risk is also known as idiosyncratic, residual, unique or unsystematic, and only affects one company/companies in a single industry. On the other hand, systematic risk is shared by most businesses: 51% of portfolio standard deviation is eliminated when diversifying from 1 to 10 securities, another ten removes 5%...
 Empirically, investors are not well diversified across assets classes and across assets within a class: Average investor in the US holds three stocks and 28% of investors only have one.
 Furthermore, these stocks tend to be highly correlated
 With N stocks, you get N estimates of variances and $\frac{N^2-N}{2}$

The variance of the portfolio returns is: $\sigma_p^2 = \frac{1}{N} * (AverageVariance) + (1 - \frac{1}{N}) * (AverageCovariance)$
 , when N goes to infinity the average variance disappears and we obtain non-diversifiable risk
 The investment opportunity set consist of all available risk-return combinations, an efficient

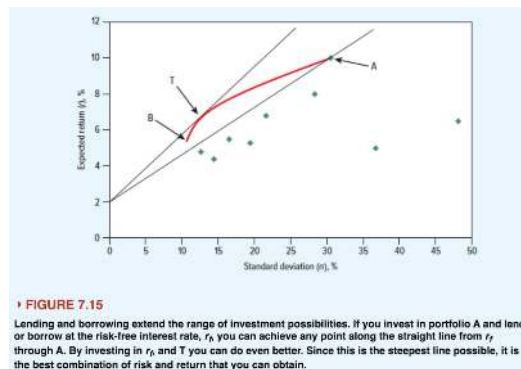
portfolio has the highest possible expected return for a given standard deviation. The set of all of them forms the efficient frontier. The Minimum Variance portfolio (MVP) is the portfolio that provides the lowest variance among all possible portfolios of risky assets

We denote the risk free return R_f : its expected value is R_f and its variance is 0. Its covariance



with any asset is 0, and R_f is constant over time.

Efficient ratios are preferable to all other portfolios, the tangency portfolio is preferable to all



other efficient portfolios. The tangency portfolio offers the highest ratio of risk premium to standard deviation: The ratio is called the Sharpe ratio: **Sharpe ratio**: $r_s = \frac{\text{risk premium}}{\text{standard deviation}} = \frac{r_p - r_f}{\sigma_p}$

Two fund separation theorem: Create the set of possible mean-s.d. combinations from different portfolios of risky assets and find the tangency portfolio (the one with the highest Sharpe ratio). Then, choose the combination of the tangency portfolio and the risk-free asset to suit your pref-



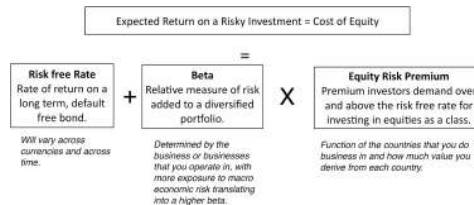
ferences

All investors hold a combination of the risk-free asset and the tangency portfolio (market portfolio), their risk aversion determines the fraction of wealth invested in the risk-free asset.

Lending means taking a long position in a risk-free asset and borrowing a short one

11 LECTURE 12: CAPM

The CAPM helps us determine the equilibrium expected return of a **risky asset**:



The relevant measure of risk for a security is $\beta_i = \frac{\text{cov}(\tilde{R}_i, \tilde{R}_m)}{\sigma^2(\tilde{R}_m)}$ and the expected return is $E(\tilde{R}_i) = r_f + \beta_i E(\tilde{R}_m) - R_f$

Important: the volatility of a security's return is not the relevant measure of risk of an individual stock. High variance of its returns could add relatively little risk to a portfolio if that volatility is diversifiable, which is the relevant risk according to the CAPM

Market portfolio: portfolio of all assets in the economy and beta (Sensitivity of a stock's return to the return on the market portfolio). Beta is a measure of the non-diversifiable risk for any asset. Assumptions of the CAPM, all investors:

- Aim to maximize economic utilities
- Are rational and risk-averse
- Are broadly diversified across a range of investments
- Are price takers
- Can lend and borrow unlimited amounts under the risk-free rate of interest
- Trade without transaction/taxation costs
- Deal with securities that are all highly divisible into small parcels
- Assume all information is available at the same time to all investors

The standard market model regression has one independent variable (simple regression): $R_{it} = \alpha_i + \beta_i R_{mt} + \epsilon_{it} \quad t = 1, \dots, T$

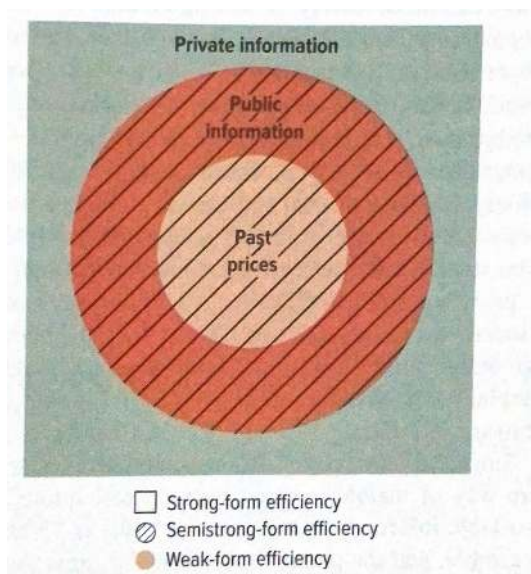
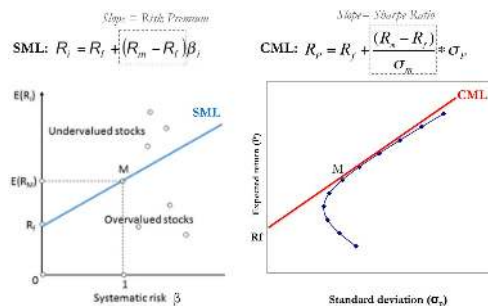
When determining beta, three elements must be taken into account: The choice of the index, the regression period and the return interval/frequency

Ideally the security that reflects the risk-free rate should have no covariance with the market/ a beta of zero

The expected return-beta relationship is represented graphically by the security market line, with the slope the risk premium. According to the CAPM, all assets are priced to lie on the SML, i.e. the price of any security adjusts until the security lies on the SML. Those above the SML are Un-dervalued (too high return considering their risk) and vice-versa

A non parallel shift reflects a change on the risk premium and a parallel shift reflects a change in the market due to a change in interest rate. For example, a cut in interest rates normally leads to a downwards shift

SML and CML:



12 LECTURE 12

Weak form efficiency defines available information as information contained in past prices. Any information contained in those is incorporated in the current price, so knowing these prices doesn't help predict future returns. So:

What happened in the past is irrelevant as markets have no memory, stock prices follow random walks and technical analysis (using stock prices to devise trading strategies) does not produce any excess returns.

Semi-strong efficiency: The market incorporates all information in past prices and public information (already reflected in the current stock price)

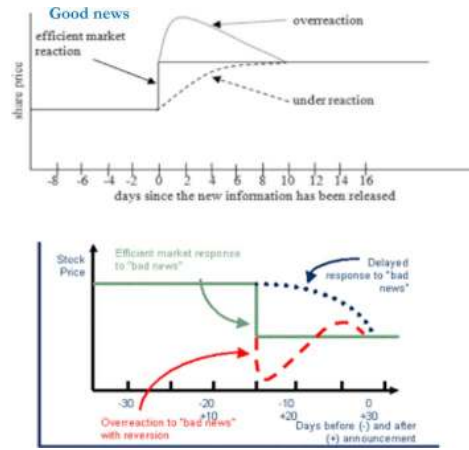
If markets are semi-strong form efficient, then fundamental analysis does not produce excess returns

Strong efficiency: all public and private information: Even insiders can't make money

The notion of informationally efficient market means that any price change must reflect new info. Hence, one should be able to measure the value of a news event by examining price changes in a time-window around the event. An event study describes a technique of empirical financial research that enables an observer to assess the impact of a particular event on a firm's stock price. However, isolating the part of a stock movement that is attributable to a specific event is complicated

The general approach starts with a proxy for what the stock return would have been like without the event. The abnormal return is the difference between this and the actual return.

Several methodologies to estimate benchmark return: Market model: The market model parameters, intercept and the slope, can be estimated via ordinary least squares regression over the estimation window. Another approach uses an asset pricing model such as the CAPM



Under CAPM $AR_t = r_t - R_t = r_t - [R_f + \beta(R_{tM} - R_f)]$, and assuming the risk free rate is 0 (narrow time window) we get $AR_t = r_t - \beta R_{tM}$

The process: Calculate daily abnormal returns in the days surrounding the announcement of the event being studied. Can be calculated using the benchmarks like the market model or an equilibrium asset pricing model (CAPM)

This study uses the statistical market model to estimate expected returns. We can then compare those to actual returns to find daily abnormal returns

The market model posits that the only factor determining the return on stock i, at time t, is the return on the market at time t. This relation is modeled linearly, as in the following equation:

$E(R_{i,t}) = b_0 + b_1 \cdot E(R_{M,t})$. Once we have our estimates of b_0 and b_1 we can find predicted returns in our event windows by plugging in the market return

Widely accepted tool, used by the SEC to measure illicit gains and fraud cases

13 LECTURE 13-14

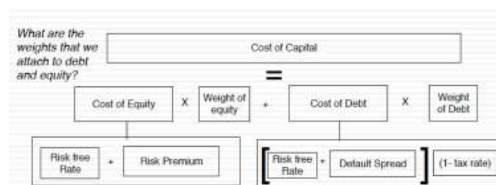
$$r_{\text{assets}} = \text{COC} = r_{\text{debt}} \left(\frac{D}{V} \right) + r_{\text{equity}} \left(\frac{E}{V} \right)$$

with r_{debt} the YTM on bonds and $r_{\text{equity}} = r_f + \beta(r_m - r_f)$

and E, D and V the market values of equity, debt and total firm value

Cost of capital serves as the opportunity cost for investors, the cost of financing for a company and the hurdle rate for investment analysis

The average beta of the assets is based on the % of funds in each asset: The expected return on a



risky investment is the cost of equity. It is equal to the risk-free rate (varies across currency and time) + the beta (relative measure of risk added to a diversified portfolio) * the equity risk premium. (function of the countries you operate in and the value derived from each country)

To estimate the ERP, three approaches:

Historical premiums (assume the actual premium delivered over time is equal to the expected periods- i.e. use historical data)

Survey Premiums: Survey investors on their desired risk premium and use the average

Implied premiums: Estimate a forward looking premium using today's asset prices

Historical ERP requires to use a long term, consistent with the choice of risk-free rate



Survey premiums issues: Finding a subset of investors that reflects the aggregate market well, the survey results are more reflective of the past than the future and they tend to be short term (not above one year)

Implied Premiums: If you know the price paid for an asset and have estimates of the expected cash flows on the asset, you can estimate the IRR of these cash flows. If you paid the price, this is your expected return

On a risk free asset, the actual return is equal to the expected return => No variance on the expected returns. For an investment to be risk-free, two conditions: no default risk (generally issued by the government) and there is no uncertainty about reinvestment rate, which implies that it's a zero coupon bond security with the same maturity as the CF being analyzed

Remember that the risk free rate or the analysis must be in the same currency as the CF
Since the risk-free rate for a portfolio is the standard deviation of the portfolio's returns, we now

want to determine the relevant measure of risk for an individual security in a portfolio
There is a trade-off between a long time series and a reliable beta estimate:

1. Careful: the dependent variable is the stock return, the explanatory variable is the market return
2. Careful: Never regress prices on prices (always regress returns on returns)
3. Careful: Returns should be based on prices adjusted for stock splits and dividends (see Session 2 What do real firms look like)
4. Careful: Fractions of the market portfolio should be value-weighted stock market indices, such as the CRSP NY Market Return, or the SP500
5. Careful: You need a lot of data (i.e. long time series) to reliably estimate betas:
 - a. One way to achieve this is to use a low data frequency (e.g. monthly returns) and go back far in time (e.g. 5 years)—the downside here is that the true relationship between the stock and the market may have changed
 - b. Another way to achieve this is to use a high data frequency (e.g. daily returns) and consider only the recent past (e.g. 1yr)—the downside here is that higher frequency data may be subject to illiquidity bias, or represent non-representative time periods
6. Careful: We do not observe the true betas, we only observe estimates; the quality of estimates, indicated by standard errors, may be lower than we would like

To avoid biases due to changes in the industry or firm, we generally use a historical period between 2 and 5 years long. The returns (market and stock) should be calculated considering both the capital gains and the dividends received. Frequency: daily is good. The market index: Due to the emergence of internationally diversified investors who use different markets, it is more and more common to calculate beta using international indices (Morgan Stanley Capital Index i.e.)

1. Choose a market index (links to the market risk premium estimation process)
2. Choose an estimation period (length of period and specific dates)
3. Choose the periodicity for the stock return (daily, weekly, or monthly interval)
4. Collect the necessary data and estimate the market model
5. Make adjustments, if any, for mean reversion and other effects

The standard procedure for estimating betas is to regress stock returns (R_j) against market returns (R_M): $R_j = +bR_M$. The slope corresponds to the beta and measures the riskiness. The risk

of any asset is the risk that it adds to the mkt portfolio: $\beta_j = \frac{Cov(R_j, R_M)}{\sigma^2(R_M)}$

Beta is a standardized measure of this covariance, it is a measure of the non diversifiable risk for any asset can be measured by the covariance of its returns with returns on a market index

We are confident at 68% percent that the true value of beta falls within one standard deviation

- The standard approach to estimating betas is to run a regression of returns of an individual stock against returns on a market index. Which of the following is a problem with this approach?
- a. It yields an estimate with significant standard error.
 - b. It is subject to estimation choices: different regression periods, return intervals and market indices.
 - c. It will not yield a "good" estimate for the future, if a company's business mix has changed recently.
 - d. It will not yield a "good" estimate for the future, if a company's financial leverage has changed over the regression period
 - e. All of the above.

and 95% within 1.96

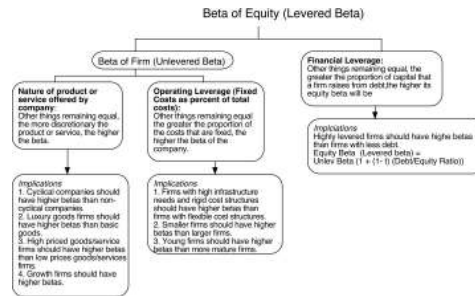
When doing a beta analysis, R squared is the market risk and 1-R squared is the unique risk

Unique variance is Variance*Unique risk

Confidence Level= Estimate+/- 1.96*SE

The firm-specific risk is diversifiable and will not be rewarded.

Projects that have the same risk as the company' existing assets can be discounted at the WACC.



It takes into account the tax benefits of debt financing

In practice, we generally obtain the CAPM empirically

The cost of capital of a firm reflects its systematic risk and not idiosyncratic risk.

14 LECUTRE 15

Dividend decision: How much to return and how

Measures of policy: $DPS = \frac{Dividends}{N \cdot Shares}$

EPS: $\frac{NetIncome}{N \cdot Shares}$

Dividend payout: $\frac{Dividends}{NetIncome}$

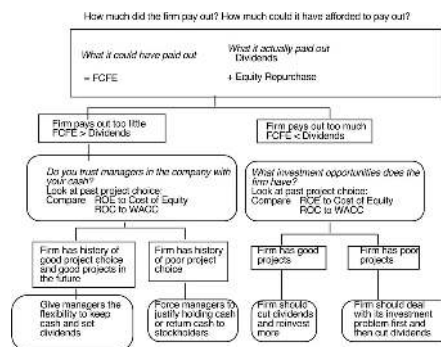
Dividend yield: $\frac{DPS}{StockPrice}$: Measures the return that an investor can make from dividends alone

The free CF to Equity (FCFE) is a measure of how much cash is left in the business after non-equity claimholders (debt and preferred stock) have been paid and after any reinvestment needed to sustain the firm's assets and future growth

Net Income

- + Depreciation & Amortization
- Capital Expenditures
- +/- Change in Working Capital
- + New Debt Issues
- Debt Repayments
- = FCFE

If a company does not have excess cash, and/or has several good investment opportunities, re-



turning money to stockholders (dividends or stock repurchases) is bad. Cash can also be kept to increase cash reserves

The benefit of a buyback is that it reduces the number of shares outstanding for a company, increasing per-share measures of profitability and measures like ROE



Dividend: A pro rata distribution to shareholders that is declared by a firm's board of directors and may or may not require approval by shareholders.: Can be paid in cash or stock. A stock dividend is essentially the same as a stock split

Repurchased shares become treasury stock (non voting, non dividend) 4 ways: buy shares on the market (95% of them)

Tender offer: firm offers to buy shares at a prespecified price during short time period (usually 20 days and 10-20% premium)

Dutch auction: the firm lists different prices at which it is prepared to buy shares, and shareholders in turn indicate how many shares they are willing to sell at each price. The firm then pays the lowest price at which it can buy back its desired number of shares

Private negotiation: directly from a specific shareholder

Greemail is the practice of buying enough shares to threaten a hostile takeover, forcing the company to repurchase its shares as a premium

Four dates for dividends: Declaration date, ex-dividend date (Shares start to trade ex-dividend), the record date (Dividends are paid to shareholders registered on that date, one day after ex-

dividend date), payment date

Empirically, the price drop is less than the dividend and occurs in a few minutes of the ex-date. In a perfect capital market, an open market share repurchase has no effect on the stock price, and it's the same as the cum-dividend price if dividends were paid instead

Stock buy backs are increasingly popular in the US

Managers do not want to reverse dividends change and smooth out their flow instead

Empirical evidence on the message contained in a dividend change is mixed, the first dividend payment signals good earnings prospects, dividends increase lead to a +% in stock and ceasing dividend leads to an announcement effect of -9.5%

Dividends are sticky and tend to follow earnings

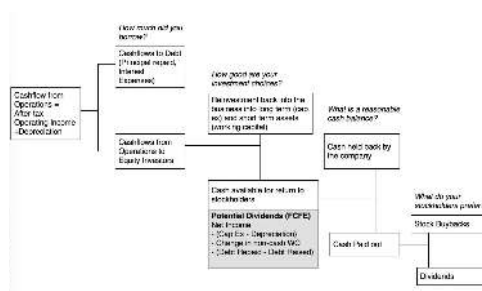
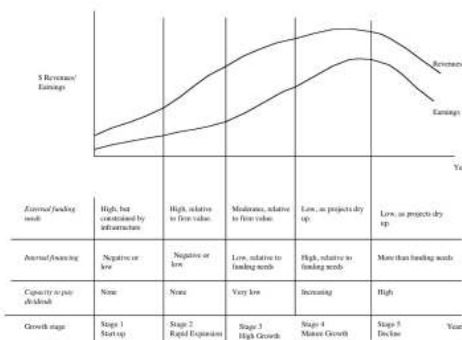
Recap: Dividend initiations increase prices and predict earnings increase (43% on average), dividends increases predict safer earnings, cuts are associated with price drops

An important question is whether payout change the value of the stock: According to Modigliani-Miller's view it is irrelevant, according to others one or the other increases value. Some argue dividend payout increase value due to high demand for dividend paying stocks, whereas tax treatment is more favourable for share repurchases

Miller and Modigliani: No taxes, transaction costs and other imperfections. We also keep constant the investment and borrowing choices. MM published proof that the payout policy is irrelevant in the absence of imperfections (taxes, transactions costs...). Fixing investments, a firm can increase dividends by issuing equity or decrease dividends by buying shares back

If dividends are taxed more heavily than capital gains, taxpaying investors should welcome share repurchases instead of dividends (historically the case in the US)

Why dividends?: Some institutions' mandates require them to hold stocks that pay dividends, trust and endowments may have restriction on selling their assets, some investors (especially elderly) appreciate a steady source of cash flows from dividend paying stocks, some investors have self-control problem, dividend make it harder for managers to waste money...



Increasing payouts is a good decision when these three conditions are met: The firm’s debt ratio is prudent, the company’s holdings of cash are a sufficient cushion for unexpected setbacks and enough for unexpected opportunities, the company is generating positive free cash flows after making all investments with a positive NPV and those cash flows are likely to continue. The two dominant factors driving dividend policy are inertia and me too-ism: Companies want to behave like their peer group.

15 LECTURE 16

Financing decisions: Finding the right mix and the right kind of debt (matches the tenor of assets) Modigliani and Miller argue that in perfect capital markets, the firm is unaffected by its capital structure. This is because **fairly priced** securities are zero-NPV projects. In perfect capital markets, the firm value is independent of its capital structure.

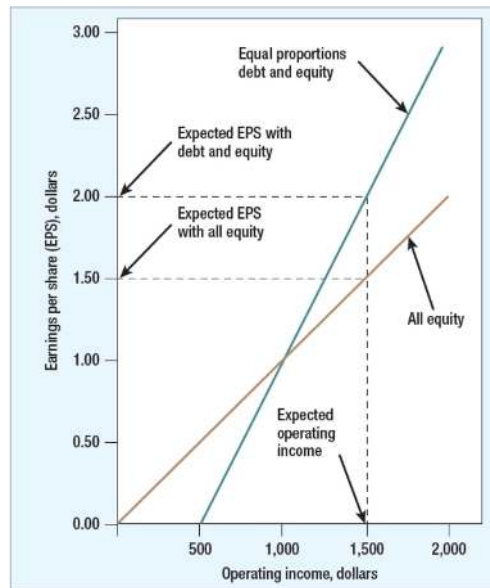
Fricitionless capital markets mean:

- No taxes
- No bankruptcy costs or other costs of financial distress
- No agency problems between managers and shareholder
- No asymmetric information between firms and investors
- No transaction costs or issuance costs
- Firms and investors with identical borrowing and lending costs

Law of one price: Two investments with the same payoffs must have the same price, and the value of the unlevered firm must equal the value of the levered firm. Law of the Conservation of value: the value of an asset is the same regardless of the nature of the



claims against it. Thus, the firm's value is determined by real assets on the left-hand side of the balance sheet.



Leverage increases the EPS but not the price, because the change in earning is offset by the change in the discount rate:

$$\text{Expected return on Asset} = \frac{\text{Expected OI}}{\text{Market value of all securities}} \Rightarrow r_a = \left(\frac{D}{D+E} \times r_D\right) + \left(\frac{E}{D+E} \times r_E\right) \Rightarrow r_e = r_a + (r_a - r_d) \times \frac{D}{E}$$

MM proposition 2: A levered firm's expected ROE increases with the D/E ratio expressed in market values

The rate of increase depends on the spread between the expected ROA and the return on debt

Overall, we can say that investors require a higher rate of return due to increased financial risk.

The beta asset is the weighted average of the debt and equity betas: $\beta_A = \left(\beta_D \times \frac{D}{V}\right) + \left(\beta_E \times \frac{E}{V}\right)$ and

$$\text{so } \beta_E = \beta_A + (\beta_A - \beta_D) \frac{D}{E}$$

Borrowing creates financial leverage which pushes Common stock risk higher, leading to **share-holders** demanding a higher return

The tax benefit from interest expense deductibility must be included, it reduces the effective cost of debt by the marginal tax rate:

$$\text{WACC} = \left[r_D \times (1 - T_c)\right] \times \left(\frac{D}{V}\right) + \left(r_E \times \frac{E}{V}\right)$$

"MM also show that both the expected return on equity and EPS increase with leverage. And yet, this does not increase firm value, as it merely compensates investors for the increase in risk brought about by the increase in leverage."

16 LECTURE 17

The simple MM model lacks corporate and personal taxes, as well as the costs of financial distress, transaction costs for issuing debt or equity and asymmetric information about the firm's investments

In reality, bankruptcy is expensive, slow and painful, and conflicts of interest between different stake holders of the firm are frequent and severe



The interest tax shield is equal to the tax rate time the interest

$$\text{Its PV is } PV(\text{tax shield}) = \frac{\text{Annual tax shield}}{\text{Interest rate on debt}} = \frac{T_C(r_D \times D)}{r_D} = T_C \times D$$

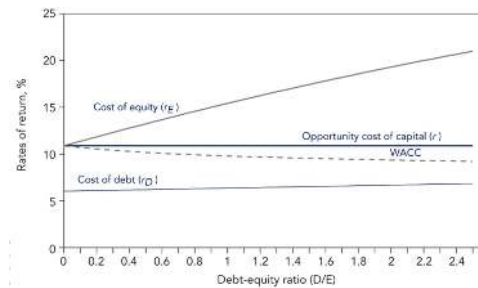
An assumption is that the risk of the tax shields is the same as that of the interest payments generating them.

Hence, $Value_{firm} = Value_{All\text{-}Equity\text{-}financed} + PV(\text{Taxshield})$

If debt is fixed and permanent: $Value_{firm} = Value_{All\text{-}Equity\text{-}Financed} + T_C D$

Caveats: Debt may not be fixed and perpetual, no interest tax shields unless there are sufficient profits, the amount of interest that can be deducted is limited to 30% of EBIT.

Money that is paid out as equity income is further taxed through personal taxes so for 1 dollar



paid out, the final income is $1 - T_C - T_{PE} * (1 - T_C) = (1 - T_C)(1 - T_{PE})$ to stockholder, and $1 - T_P$ for bondholders

Relative advantage formula: $\frac{1 - T_P}{(1 - T_{PE})(1 - T_C)}$. If it's above 1, debt has the advantage and Equity if below 1

The main advantages of debt are tax benefits and added discipline (borrowing money may force managers to think more about the consequences of the investment decisions a little more carefully and reduce bad investments)

The disadvantages of debt are Expected bankruptcy cost (Expected cost of going bankrupt * Probability). This includes both direct and indirect costs. The probability of going bankrupt is higher in businesses with more volatile earnings. This means firms with more stable earnings should borrow more for a given level of earnings, and so should firms with lower bankruptcy costs Agency costs are another issue, as action that benefit equity investors may hurt lenders. The greater the potential for this conflict of interest the greater the cost borne by the borrower (higher interest rates/more covenants). Finally, there's a loss of flexibility, as using up available debt capacity today will mean you can't draw on it in the future. Hence, the better you can forecast future funding needs should be able to borrow more, and those with better access to capital markets should be more willing to borrow more today

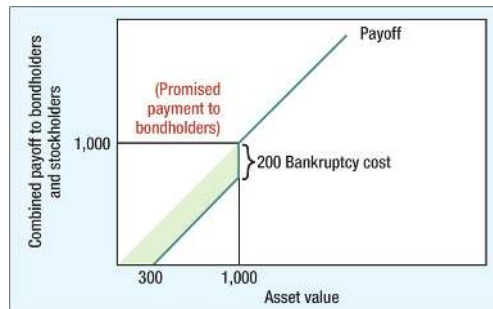
Direct bankruptcy costs include legal and accounting fees, but also the loss of customers (if you

sell in advance especially), loss of suppliers and loss of employees

We now get: $Value_{Firm} = Value_{All\text{-}Equity\text{-}Financed} + PV(\text{Tax Shield}) - PV(\text{costs of financial distress})$ and

Management represents equityholders' interests are amplified when firms enter financial distress

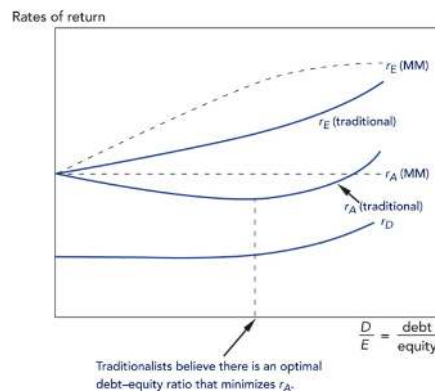
Risk shifting (management invests in risky projects with a negative NPV), Underinvestment: A leveraged company foregoes investment opportunities because debt holders capture too much of the value of the project, leaving insufficient returns for shareholders. Finally, cash in and run is when stakeholders take the money out



Overall, to optimize, there **three approaches**: Cost of Capital, Life Cycle and Sector. The first indicates that the optimal mix is the one that minimizes the cost of capital for a firm, the second that the optimal debt ratio is the one that best suits where the firm is in its life cycle and finally, the sector approach: The optimal debt ratio is the one that brings the firm closest to its peer group in terms of mix.

Large firms tend to have higher debt ratios, firms with high ratios of fixed assets to total assets have higher debt ratio, market to book: Firms with higher ratios of MTB value have lower debt ratios and profitability, more profitable firms have lower debt ratios

Important: Cost of equity!≠ Cost of capital, it is not the return you hope to make, it is not a mechanism to reverse engineer a desired rate and it is not constant



17 LECTURE 18

Valuing and pricing an assets are two different things: The drivers of intrinsic value are cashflows from existing assets, growth in CF and its quality, whereas drivers of price are market moods and momentum and surface stories about fundamentals

The first one we use DCF, the second one relative valuations using multiples.

A publicly traded firm potentially has an infinite life, so Value = $\sum_{t=1}^{t=\infty} \frac{CF_t}{(1+r)^t}$. Since we can't estimate cash flows forever, we estimate cf for a growth period and then estimate a terminal value to capture the value at the end of the period

The market value of equity is Cash and other non-operating assets+ Operating assets - debt

How to account for the value of a financing decision: adjust the discount rate to the new after-tax WACC and adjust the present value: Start with a NPV from an all equity financed firm and add/subtract the value of financing decisions: APV= base case value + value of financingside effects



The assumptions behind using the wacc as a discount rate are that risk and leverage stay constant

Remember that tax shields are accounted for in the after-tax WACC: $PV = \frac{FCF_1}{(1+WACC)^1} + \frac{FCF_2}{(1+WACC)^2} +$

$$\dots + \frac{FCF_H}{(1+WACC)^H} + \frac{PV_H}{(1+WACC)^H}$$

When computing acquisition value for an M&A, use the WACC of the target

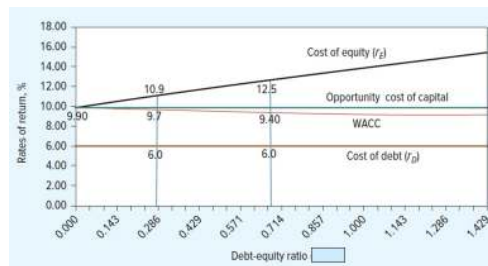
FCF and NI differ: Incoem is computed after interest expense, while FCF assumes all equity financing, Income accounts for non cash expenses, Investments in fixed assets and working capital reduce cash flows but do not appear in the IS

When we include more sources of financing, we simply expand the WACC formula $WACC =$

$$(1 - Tc) \left(\frac{D}{V} \times r_D \right) + \left(\frac{P}{V} \times r_P \right) + \left(\frac{E}{V} \times r_E \right)$$

Using industry WACC is more appropriate for multidivisional firms. if a company can't use all its interest tax shields, if it's temporary you ignore it, if it's permanent you use the APV method

The required return on assets is the opportunity cost of capital



Unlevering and relevering beta: 1) Unlever beta 2) Estimate the beta of debt and equity at the

new debt ratio 3) Recalculate the cost of equity and the WACC at the new financing weight When calculating the PV of financing impact, we look at all costs/benefits directly resulting from

financing: Interest tax shields (+), cost of securities (-), Subsidized debt (+)

If we assume that debt is a constant proportion of the value, then the risks of the tax shield is the same as the one of the project, if we assume it has the same risk as the debt then. One advantage of APV is that we do not need to assume that Debt is a constant proportion of value LBOs are takeovers typically of mature companies, heavily debt-financed. The new debt is not intended to be permanent. LBO business plans call for generating extra cash by selling assets, shaving costs and improving profit margins. Therefore, you can't use a single WACC as a discount rate to evaluate an LBO because its debt ratio will not be constant

APV work well for LBO. The company is first seen as fully equity financed. Then, tax shields are valued separately and added to the all equity value, also,ng with other financing side effect.

FOR DOUBTS OR SUGGESTIONS ON THE HANDOUTS



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